

$$1. \int_{-9}^9 \int_{-\sqrt{81-y^2}}^{\sqrt{81-y^2}} \int_{-\sqrt{81-x^2-y^2}}^{\sqrt{81-x^2-y^2}} f(x, y, z) dz dx dy$$

$$2. 364$$

$$3. 6 - 2 \ln 4$$

$$4. \int_0^1 \int_0^{12} \int_0^{\frac{x}{4}} \frac{4 \cos(x^2)}{5\sqrt{z}} dy dx dz = \frac{1}{5} \sin 144$$

$$5. \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \int_0^3 \int_0^2 e^{-r^2} r dz dr d\theta = \frac{\pi}{4} (1 - e^{-9})$$

$$6. \int_0^{2\pi} \int_0^4 \int_{\sqrt{25+x^2+y^2}}^{\sqrt{41}} r dz dr d\theta = -\frac{34}{3} \pi \sqrt{41} + \frac{250}{3} \pi$$

$$7. \int_0^{2\pi} \int_0^{\pi} \int_0^2 7e^{-\rho^3} \rho^2 \sin \phi d\rho d\phi d\theta = \frac{28\pi}{3} (1 - e^{-8})$$

$$8. \left( \bar{x}, \bar{y} \right) = \left( \frac{M_y}{m}, \frac{M_x}{m} \right) = \left( \frac{8}{21}, \frac{22}{21} \right)$$

$$9. \left( \bar{x}, \bar{y}, \bar{z} \right) = \left( \frac{M_{yz}}{m}, \frac{M_{xz}}{m}, \frac{M_{xy}}{m} \right) = \left( \frac{8}{3}, \frac{11}{21}, \frac{4}{3} \right)$$

10. B

11. One correct answer is  $\langle 0, y \rangle$ .

$$12. \left\langle \frac{8x}{4x^2 + y^2 + 4z^2}, \frac{2y}{4x^2 + y^2 + 4z^2}, \frac{8z}{4x^2 + y^2 + 4z^2} \right\rangle$$

$$13. \sqrt{65} \int_{-2\pi}^0 (8 \sin t - t) dt = 2\pi^2 \sqrt{65}$$

$$14. 32\sqrt{2} \int_0^1 \frac{1}{2(1+32t)} dt = \frac{\sqrt{2}}{2} \ln 33$$

15. Circulation is 0. Flux is  $-25\pi$ .

16. Conservative,  $\phi(x, y, z) = 2xyz$

$$17. \phi\left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right) - \phi(0, 1) = \frac{\sqrt{3}}{4}$$

$$18. \frac{10}{9}$$

19. 0, because the vector field is conservative.

20. Two-dimensional curl of  $\mathbf{F}$  is  $8y^3 + 50x^6$ . The two-dimensional divergence is  $36x^5y + 24xy^2$ .

$$21. \int_0^{\pi} \int_0^{\sin x} (18x^2 - 8xy) dy dx = 17\pi^2 - 72$$

$$22. \int_0^{\frac{\pi}{2}} \int_0^{\frac{\pi}{2}} (-y \sin x - 0) dy dx = -\frac{\pi^2}{8}$$

$$23. \operatorname{div} \mathbf{F} = -4xyz$$

$$24. \operatorname{curl} \text{ of } \mathbf{F} = \langle 0, 0, 4y \rangle$$