1. Write an iterated integral for $\iiint_D f(x, y, z) dV$ where D is a sphere of radius 9 centered at

(0,0,0) using the order dz dx dy.

- 2. Evaluate the integral $\int_{-1}^{3} \int_{2}^{5} \int_{1}^{e} \frac{x^2 y^2}{z} dz dx dy$.
- 3. Set up and then use a triple integral to find the volume of the solid bounded by the surfaces $z = 2e^{y}$ and z = 2 over the rectangle $\{(x, y) | 0 \le x \le 1, 0 \le y \le \ln 4\}$.



- 4. Evaluate the integral $\int_0^1 \int_0^3 \int_{4y}^{12} \frac{4\cos(x^2)}{5\sqrt{z}} dx dy dz$ by rewriting the order of integration inn an appropriate way.
- 5. Evaluate the following integral in cylindrical coordinates $\int_{0}^{2} \int_{0}^{\frac{3\sqrt{2}}{2}} \int_{x}^{\sqrt{9-x^{2}}} e^{-x^{2}-y^{2}} dy dx dz$
- 6. Use cylindrical coordinates to find the volume of the region bounded by the plane $z = \sqrt{41}$ and the hyperboloid $z = \sqrt{25 + x^2 + y^2}$.



- 7. Find the mass of the ball of radius 2 centered at the origin with a density of $f(\rho, \varphi, \theta) = 7e^{-\rho^3}$.
- 8. Find the center of mass of the triangular plate in the first quadrant bounded by y = x, x = 0, and y = 2 x with $\rho(x, y) = 18x + 6y + 9$.

- 9. Find the center of mass for the interior of the prism formed by z = x, x = 4, y = 1 and the coordinate planes with density $\rho(x, y, z) = 3 + y$.
- 10. Which of the following is a vector field for $\mathbf{F} = \langle 2y, 2x \rangle$?



- 11. Give an example of a component vector field F on \mathbb{R}^2 where F is everywhere normal to the line y = 3.
- 12. Find the gradient field $F = \nabla \varphi$ for the potential function $\varphi(x, y, z) = \ln(4x^2 + y^2 + 4z^2)$.
- 13. Integrate the line integral $\int_{C} (y-z) ds$ where *C* is the helix $\langle 8\cos t, 8\sin t, t \rangle$ with $-2\pi \le t \le 0$.
- 14. Integrate the line integral $\int_{C} \frac{x}{x^2 + y^2} ds$ where *C* is the line segment from (1,1) to (33,33).
- 15. Consider the vector field $\mathbf{F} = \langle y x, x \rangle$ and the curve $C : \mathbf{r}(t) = \langle 5\cos t, 5\sin t \rangle$ for $0 \le t \le 2\pi$. Find the circulation and the flux.
- 16. Determine if $F = \langle 2yz, 2xz, 2xy \rangle$ is a conservative vector field on \mathbb{R}^3 . If so, find the potential function $\varphi(x, y, z)$.
- 17. Evaluate the line integral $\int_{C} \nabla \varphi \cdot d\mathbf{r}$ using the Fundamental Theorem for line integrals where π

$$\varphi(x, y) = xy$$
 and $C: \mathbf{r}(t) = \langle \sin t, \cos t \rangle$ for $0 \le t \le \frac{\pi}{3}$.

18. Evaluate the line integral $\int_{C} \nabla \varphi \cdot d\mathbf{r}$ using the Fundamental Theorem for line integrals where

$$\varphi(x,y,z) = \frac{x^2 + y^2 + z^2}{2} \text{ and } C: \mathbf{r}(t) = \left\langle \cos t, \sin t, \frac{t}{\pi} \right\rangle \text{ for } \frac{\pi}{6} \le t \le \frac{3\pi}{2}.$$

- 19. Evaluate $\oint_{C} \mathbf{F} \cdot d\mathbf{r}$ for the vector field $\mathbf{F} = \langle -x z, y + z, y x \rangle$ and the closed curve $C : \mathbf{r}(t) = \langle -\sin t, -\sin t, \cos t \rangle$ for $0 \le t \le 2\pi$.
- 20. Assume *C* is a circle centered at the origin, oriented counterclockwise, that encloses disk *R* in the plane. Find both the two-dimensional curl of F and the two-dimensional divergence of F given $F = \langle 6x^6y, 8xy^3 + 8x^7 \rangle$.
- 21. Use Green's Theorem circulation form to evaluate $\oint_C \mathbf{F} \cdot d\mathbf{r}$, where $\mathbf{F} = \langle 4xy^2, 6x^3 + y \rangle$ and C is oriented counterclockwise and is the boundary of $\{(x, y) | 0 \le y \le \sin x, 0 \le x \le \pi\}$.
- 22. Compute the outward flux of $F = \langle y \cos x, -\sin x \rangle$ across the boundary of R which is oriented
 - counterclockwise. R is the square $\left\{ (x, y) \middle| 0 \le x \le \frac{\pi}{2}, 0 \le y \le \frac{\pi}{2} \right\}$.
- 23. Find div F for the vector field $F = \langle 2x^2yz, -2xy^2z, -2xyz^2 \rangle$.
- 24. Compute the curl of F = $\langle 2x^2 y^2, 2xy, z \rangle$