1. Consider the parametric equations: $\frac{x = (t+3)^2}{y = t+7}$ for $-10 \le t \le 10$. Eliminate the

parameter. Describe the curve and indicate the positive orientation by stating the starting ordered pair and the ending ordered pair.

- 2. Consider the parametric equations: $x = 6\cos t$ $y = 6\sin t$ for $\pi \le t \le 2\pi$. Eliminate the parameter. Describe the curve and indicate the positive orientation by stating the starting ordered pair and the ending ordered pair.
- 3. Find parametric equations for the complete curve $x = -4y^3 y$, include the interval for the parameter.
- 4. Find parametric equations for the line segment that moves from (-4, -2) to (2, 4), include the interval for the parameter.
- 5. Find $\frac{dy}{dx}$ for the parametric curve $\begin{cases} x = 3t \\ y = t^5 \end{cases}$ then evaluate $\frac{dy}{dx}$ at t = 2.
- 6. Find the equation of the tangent line to the curve given by $\begin{aligned} x &= \cos t + t \sin t \\ y &= \sin t t \cos t \end{aligned} \text{ at } t = \frac{3\pi}{4}. \end{aligned}$
- 7. Find the arc length of the curve given by $\begin{array}{c} x = 2t^3 \\ y = 3t^2 \end{array}$ where $0 \le t \le \sqrt{8}$.
- 8. Name two other ordered pairs, one with a positive r and one with a negative r that represents the same point as $\left(-3, -\frac{\pi}{3}\right)$.
- 9. Write the polar point $\left(-2, \frac{-11\pi}{6}\right)$ in Cartesian coordinates.
- 10. Write the Cartesian point $(5\sqrt{3},5)$ in polar form with $0 \le \theta \le 2\pi$.
- 11. Find $\frac{dy}{dx}$ for the polar curve $r = 7 7\sin\theta$. Then evaluate the derivative at the point $\left(14, \frac{3\pi}{2}\right)$.
- 12. Find $\frac{dy}{dx}$ and the points at which the polar curve $r = 3\cos\theta$ has a vertical or horizontal tangent line.
- 13. Find the area inside one leaf of $r = 5\cos 3\theta$.
- 14. Given the polar equations $r = 16 + 16\sin\theta$ and $r = 16 + 16\cos\theta$ find all points of intersection and the area that lies inside both curves (not just the overlapping portion).
- 15. Find the area of the region outside r = 3 and inside $r = -6\cos\theta$.

- 16. Find the length of the curve $r = \frac{20}{1 + \cos \theta}$ on the interval $0 \le \theta \le \frac{\pi}{2}$.
- 17. Given the equation of the ellipse $5x^2 + 7y^2 = 35$, write in standard form then find the coordinates of the foci and the length of both the major and minor axis.
- 18. Find an equation of the hyperbola with foci (-13,0) and (13,0); and vertices at (12,0) and (-12,0).
- 19. Find the equation of the tangent line to the curve $y^2 \frac{x^2}{64} = 1$ at the point $\left(6, \frac{5}{4}\right)$.
- 20. Given the points Q(-5,1), T(3,2), P(-2,-3), U(6,-2), R(0,-1), and S(-4,-4) find the vectors \overrightarrow{QT} , \overrightarrow{PU} , and \overrightarrow{RS} . Are any of these vectors equal?
- 21. Find a vector in the direction of $\langle 6, -8 \rangle$ that has a magnitude of 4.
- 22. An airplane flies horizontally from east to west at 282 mph relative to the air. If is flies in a steady 38mph wind that blows horizontally toward the southwest (45° south of west), find the speed and direction of the airplane relative to the ground.
- 23. Suppose you are pulling a suitcase with a strap that makes a 30° angle with the horizontal. The magnitude of the force you exert on the suitcase is 24 lb. Find the horizonal and vertical components of the force.
- 24. Find the equation of the sphere that passes through P(-8,7,8) and Q(2,-1,7) with its center at the midpoint of PQ.
- 25. Find the center and radius of the sphere $x^{2} + y^{2} + z^{2} 14x + 6y 10z + 58 = 0$.
- 26. Given the vectors $\mathbf{u} = \langle 5, 3, 7\sqrt{3} \rangle$ and $\mathbf{v} = \langle 1, 0, 8\sqrt{3} \rangle$ find the following: $4\mathbf{u} + 2\mathbf{v}$, $3\mathbf{u} \mathbf{v}$, and $|\mathbf{u} + 3\mathbf{v}|$.
- 27. Find two vectors parallel to the vector **v** with a length of 42. $\mathbf{v} = \overrightarrow{PQ}$ with P(5,5,3) and Q(4,1,8).
- 28. Given $\mathbf{u} = \mathbf{i} 2\mathbf{j} + 3\mathbf{k}$ and $\mathbf{v} = 3\mathbf{i} + \mathbf{j} + 4\mathbf{k}$, find $\mathbf{u} \cdot \mathbf{v}$ and the angle between the vectors.
- 29. Given the vectors $\mathbf{u} = \langle -7, 0, 4 \rangle$ and $\mathbf{v} = \langle 1, 2, -2 \rangle$ find $\operatorname{proj}_{\mathbf{v}} \mathbf{u}$.
- 30. Find the value of c so that the vectors $\langle 2, -3, c \rangle$ and $\langle 1, -4, -3 \rangle$ are orthogonal.
- 31. Find a vector normal to the vectors $\langle 7,0,4
 angle$ and $\langle -8,3,2
 angle$.

- 32. Find both the vector equation and the parametric equations of the line through (-3,1,4) and (4,-2,0), let t = 0 correspond to the first point.
- 33. Determine if the lines $\mathbf{r}_1 = \langle 1, 4, 3 \rangle + t \langle 7, -5, -3 \rangle$ and $\mathbf{r}_2 = \langle 7, 6, 15 \rangle + s \langle 3, 1, 6 \rangle$ are parallel, intersect at a single point, or are skew. If they are parallel determine if they are the same line (intersecting at every point). If the lines intersect at a single point, find the point.
- 34. Determine if the lines x = 2, y = 6-t, z = 1+t and x = -2-4s, y = 1+5s, z = 4-s are parallel, intersect at a single point, or are skew. If they are parallel determine if they are the same line (intersecting at every point). If the lines intersect at a single point, find the point.
- 35. Use the fact that $d = \frac{|\mathbf{v} \times \overrightarrow{PQ}|}{\mathbf{v}}$ to find the distance from the point (2, -1, 1) to the line x = -1-t, y = 1-2t, z = -6+3t.
- 36. Find the equation of the plane parallel to the vectors (2,0,3) and (0,3,3) passing through the point (3,0,-1).
- 37. Determine if the planes 4x + 4y + 2z = 23 and -4x 3y + 14z = 23 are parallel, orthogonal or neither.
- 38. Find the equation of the line where the planes 2x 3y + z = 1 and x + y + z = 0 intersect, if it exists.
- 39. Find the point, if it exists, at which the plane y = -8 and the line $\mathbf{r} = \langle 4t + 1, -t + 5, t 6 \rangle$ intersect.
- 40. Find the smallest angle between the planes 7x + 4y z = 0 and -5x + 2y + 2z = 0.
- 41. Consider the equation of the quadric surface $\frac{y^2}{36} + 100z^2 \frac{x^2}{25} = 4$. Find the equations of the xy-, xz-, and yz-traces. Identify the surface.
- 42. Write the equation $-x^2 y^2 + \frac{z^2}{4} + 8x 6y = 29$ in standard form of one of the

quadric surfaces. Identify the surface and it's center.