Algebraic Concepts
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## SHOW ALL WORK.

1. Write the equations of the lines:


2. Find $k$ if the line through the points $(2,4)$ and $(4, k)$ is to have a slope of $m=\frac{3}{2}$.
3. Write the equation of the line

4. The equation of a line is $5 x-7 y=28$ find the following:
a) the $x$ intercept (as an ordered pair)
b) the $y$ intercept (as an ordered pair)
c) the slope of the line $5 x-7 y=28$
d) the equation of the line perpendicular to $5 x-7 y=28$ that passes through $(1,-6)$. Write answer in both slope intercept form as well as standard form.
e) the equation of the line parallel to $5 x-7 y=28$ that passes through $(1,-6)$.

Write answer in both slope intercept form as well as standard form.
f) Graph the line $5 x-7 y=28$
5. Write the equation of the line given the following information. Leave answers in slope intercept form, when possible.
a. passes through the points $(7,-5)$ and $(-3,-5)$
b. passes through the points $(-1,8)$ and $(-6,2)$
c. $m=-\frac{5}{4}$ and passes through $(16,-1)$
d. $m$ is undefined and passes through $(-3,-5)$
e. $m=\frac{2}{3}$ and it passes through $\left(-\frac{3}{4}, \frac{2}{5}\right)$

Solve the following systems of equations by the method of your choice. If there is a unique solution give it as an ordered pair or ordered triple. If there are infinitely many solutions or no solutions state that.
6. $3 x-3 y=6$
$2 x-2 y=-4$
7.

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7 x-3 y=4
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2 x+5 y=7
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8. $\frac{1}{3} x+\frac{1}{4} y=1$

$$
x-\frac{3}{2} y=4
$$

9. $\frac{1}{3} x+\frac{1}{4} y=4$

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3 x-4 y=0
$$

$$
-x+y+3 z=6
$$

10. $x+y+2 z=7$
$2 x+3 y+z=4$
11. 

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\begin{array}{r}
2 x-5 y=1 \\
-4 x+10 y=6
\end{array}
$$

12. A mixture of $8 \%$ disinfectant solution is to be made from $10 \%$ and $7 \%$ disinfectant solutions. How much of each solution should be used if 30 gallons of $8 \%$ solution are needed?
Set up the system of equations and solve by the method of your choice.
13. The Little Town Fine Arts Center charger $\$ 21$ per adult and $\$ 10$ per senior citizen for its performances. On a recent weekend when 559 people paid admission, the total receipts were $\$ 7493$. How many who paid were senior citizens? Set up the system of equations and solve by the method of your choice.
14. Solve the following systems of inequalities. Clearly indicate where the solution lies on the graph.
a) $\begin{aligned} & y \geq 2 x-1 \\ & x+y \leq-2\end{aligned}$
y<3x+2
b) $y \leq-\frac{3}{4} x$
